

# Video-rate laser Doppler vibrometry by heterodyne holography

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We report a demonstration video-rate heterodyne holography in off-axis configuration. Reconstruction and display of a one megapixel hologram is achieved at 24 frames per second, with a graphics processing unit. Our claims are validated with real-time screening of steady-state vibration amplitudes in a wide-field, noncontact vibrometry experiment. © 2011 Optical Society of America  
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The laser Doppler method is the most common optical interferometry technique used for noncontact measurements of mechanical vibrations. Though highly effective for single-point vibration analysis, this technique is much less adapted to wide-field imaging than holography. Homodyne [1–3] and heterodyne [4–6] holographic recordings in off-axis configuration enabled reliable measurements of mechanical vibrations, but none of them allowed real-time monitoring, which is an essential feature. Matching the display rate of optically measured megapixel digital holograms with real-time imaging standards is demanding in terms of computational power. Holographic measurements are performed in a diffraction plane. Hence, image formation requires to simulate the back propagation of an optical field. Such propagation involves turning the data measured in the plane of an array detector into a reciprocal plane with at least one bidimensional numerical Fourier transformation, typically a fast Fourier transform (FFT). Recently, the real-time display of digital holograms with graphics processing units (GPUs) [7,8] has alleviated the issue of the high computational workload needed for such image reconstruction. Parallel computations on the GPU consistently increase the throughput with respect to CPUs for computer-generated holograms, which demonstrated the performance of GPUs in streamline image processing [9,10].

In this Letter, we report an experimental demonstration of an image acquisition scheme designed to perform video-rate image reconstruction and display from heterodyne holographic measurements on a one megapixel sensor array. Image reconstruction of steady-state vibration modes of up to 100 kHz at a rate of 24 images per second is achieved. GPU processing is shown to enable holographic reconstruction and display with three FFT calculations per recorded frame, which covers the processing throughput needs of three reconstruction approaches: the convolution, angular spectrum, and Fresnel transform methods [11].

The acquisition setup consists of an off-axis, frequency-shifting holographic scheme used to perform a multipixel heterodyne detection of optical modulation sidebands. Optical heterodyning is a process for placing information at frequencies of interest (e.g., the mechanical vibration of an object under investigation) into a useful frequency range by mixing the frequency content of the probe beam with a reference (or local oscillator, LO) beam. The optical frequency of the reference beam is shifted to generate a beat frequency of the interference pattern within the sensor bandwidth, which carries the information at the original frequency of interest. The Mach-Zehnder heterodyne interferometer used for the detection of an object field  $E$  in reflective geometry, beating against a LO field  $E_{LO}$ , is sketched in Fig. 1. The main optical radiation field is provided by a 100 mW, single-mode, doubled Nd:YAG laser (Oxxius SLIM 532) at wavelength  $\lambda = 532$  nm, and optical frequency  $\omega_L/(2\pi) = 5.6 \times 10^{14}$  Hz. The optical frequency of the LO beam is shifted by an arbitrary quantity  $\Delta\omega$ , in the low radiofrequency (RF) range ( $0 \text{ Hz} \leq \Delta\omega/(2\pi) \leq 100$  kHz) by two acousto-optic modulators (AA-electronics, MT80-A1.5-VIS). The LO field has the form  $E_{LO} = \mathcal{E}_{LO} e^{i(\omega_L + \Delta\omega)t}$ , where  $\mathcal{E}_{LO}$  is its complex amplitude. The object studied is a sheet of paper, whose lateral dimensions are  $9 \times 26$  mm, shined over  $9 \times 17$  mm. It is attached to a

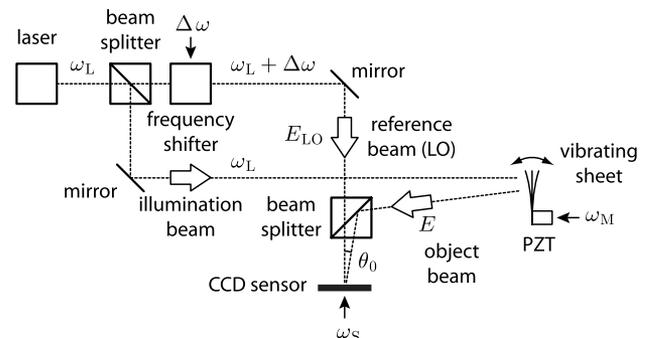


Fig. 1. Experimental image acquisition setup.

piezo-electric transducer (Thorlabs AE0505D08F), vibrating sinusoidally, driven at 10 V. Its local out of plane vibration  $z(t) = z_{\max} \sin(\omega_M t)$ , where  $z_{\max}$  is the vibration amplitude, provokes a modulation of the optical path length of the object field. It induces a local optical phase modulation of the backscattered field at the mechanical vibration frequency  $\phi(t) = \phi_0 \sin(\omega_M t)$ , where  $\phi_0 = 4\pi z_{\max}/\lambda$  is the modulation depth of the optical phase. Holographic analysis of objects in sinusoidal vibration with a frequency-shifted LO beam tuned to the  $n$ th optical modulation sideband was carried-out extensively in [4]. The frequency filtering properties of time-averaged holography were introduced in [1]. The same filtering properties were described in digital holography [12,13]. It was shown that holograms of optical sidebands could be recorded selectively by matching the frequency shift of the LO beam with the frequency of the band of interest. In the case of sinusoidal phase modulation, the hologram amplitude is of the form  $J_n(\phi_0)$ , where  $J_n$  is the  $n$ th order Bessel function of the first kind. This modulation yields fringes that correspond to local extrema of  $J_n$ . It was also shown that imaging at harmonics of the vibration frequency could enable robust assessment of vibration amplitudes, which are much greater than the optical wavelength [6]. The interference pattern  $I$  is measured with a Pike F421-B camera on a Kodak KAI-04022 interline, progressive-scan CCD sensor ( $2048 \times 2048$  pixels, pixel size  $d_{\text{px}} = 7.4 \mu\text{m}$ ). The camera is run in binning mode (an effective pixel is made of four adjacent pixels); 16 bit,  $1024 \times 1024$  pixels images are sampled at  $\omega_S/(2\pi) = 24 \text{ Hz}$  throughout the experiments described hereafter. The RF command signals at frequencies  $\Delta\omega$ ,  $\omega_M$ , and  $\omega_S$  are phase locked. The temporal part of the object field undergoing sinusoidal phase modulation can be decomposed in a basis of Bessel functions using the Jacobi-Anger identity

$$E = \mathcal{E} e^{i\omega_L t + i\phi(t)} = \sum_{n=-\infty}^{\infty} \mathcal{E} J_n(\phi_0) e^{i(\omega_L + n\omega_M)t}, \quad (1)$$

where  $\mathcal{E} J_n(\phi_0) = \mathcal{E}_n$  is the weight of the optical modulation sideband of order  $n$ , and  $\mathcal{E}$  is the complex amplitude of the field. If the frequency detuning  $\Delta\omega$  is set close to the  $n$ th modulation harmonic, i.e.,  $|\Delta\omega - n\omega_M| < \omega_S$ , and if the modulation frequency is much greater than the sampling frequency, i.e.,  $\omega_M \gg \omega_S$ , the time-averaging-induced bandpass filter of the detection process will isolate the term of order  $n$  in Eq. (1) and reject all other optical sidebands. In the sensor plane, the interference pattern of  $E$  and  $E_{\text{LO}}$  takes the form  $I(t) = |E + E_{\text{LO}}|^2 = |E|^2 + |E_{\text{LO}}|^2 + EE_{\text{LO}}^* + E^*E_{\text{LO}}$ , where  $*$  denotes the complex conjugate. The frame  $I(t)$  acquired at time  $t$  by the framegrabber is moved to a frame buffer in the GPU random-access memory by a CPU thread (Fig. 2).

To detect the heterodyne signal of interest  $EE_{\text{LO}}^* = \mathcal{E}_{\text{LO}}^* \mathcal{E}_n e^{i(n\omega_M - \Delta\omega)t}$ , a sliding four-phase temporal demodulation is performed. The intermediate frequency  $n\omega_M - \Delta\omega$  is set within the camera bandwidth to be sampled efficiently. More precisely, for an LO detuning  $\Delta\omega = n\omega_M - \omega_S/4$ , the modulation sideband  $\mathcal{E}_n$  beats at the frequency  $\omega_S/4$  (6 Hz) in  $I(t)$ . To detect it, the following quantity is formed

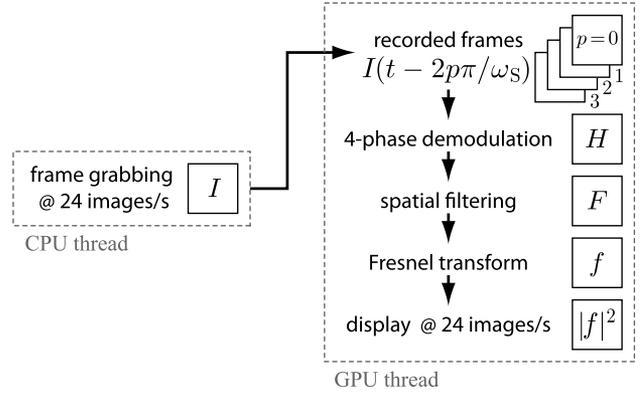


Fig. 2. Algorithmic layout of holographic rendering.

$$H(t) = \sum_{p=0}^3 I(t - 2p\pi/\omega_S) e^{ip\pi/2}. \quad (2)$$

$H$  is a complex-valued array, proportional to the diffracted field  $E$  in the sensor plane. Its calculation requires the allocation of a stack of four arrays in the GPU memory, filled with  $I(t)$ ,  $I(t - 2\pi/\omega_S)$ ,  $I(t - 4\pi/\omega_S)$ , and  $I(t - 6\pi/\omega_S)$ . Each new frame grabbed at instant  $t$ , yields a shift of the stack (Fig. 2):  $I(t)$  replaces the array  $I(t - 8\pi/\omega_S)$ .

In off-axis configuration, the spatial spectrum in the reciprocal plane  $(k_x, k_y)$  of the term  $EE_{\text{LO}}^*$  in the expression of  $I(t)$  is shifted by the projection of the wave vector difference along a transverse direction  $x$  in the sensor plane  $\Delta k_x \sim 2i\pi\theta_0/\lambda$ . Spatial filtering [14] of the time-demodulated signal  $H(t)$  in off-axis geometry is used to remove the remaining contributions of the zero-order terms  $|E|^2$  and  $|E_{\text{LO}}|^2$  and the twin-image term  $E^*E_{\text{LO}}$  to enhance the detection sensitivity. It is made by multiplying the  $(k_x, k_y)$  spectrum of  $H$  by a mask  $M$ , allowing only frequencies in the neighborhood of  $\Delta k$  to pass.

$$F(t) = \mathcal{F}^{-1}\{M\mathcal{F}\{H(t)\}\}, \quad (3)$$

where  $\mathcal{F}$  is a spatial FFT and  $\mathcal{F}^{-1}$  is an inverse spatial FFT. This operation is handled by the GPU. Only the heterodyne contribution of interest  $F(t) = \mathcal{E}_{\text{LO}}^* \mathcal{E}_n$  remains in the filtered frame.

Image rendering from  $F \propto \mathcal{E}_n$  in the sensor plane involves a scalar diffraction calculation in the Fresnel approximation, performed with a discrete Fresnel transform [15]. The hologram  $f(t)$  back propagated to the object plane is calculated by forming the FFT of the product of  $F$  with a quadratic phase map, depending on the relative curvature of the wavefronts of  $E$  and  $E_{\text{LO}}$  in the sensor plane  $(x, y)$  via a distance parameter  $\Delta z$ . This calculation is handled by the GPU.

$$f(t) = \mathcal{F}\{F(t) e^{i\pi(x^2 + y^2)/(\lambda\Delta z)}\}. \quad (4)$$

Finally, the GPU calculates the quantity  $|f(t)|^2 \propto |J_n(4\pi z_{\max}/\lambda)|^2$ , which is a map in the object plane of the composition of the local vibration amplitude field  $z_{\max}$ , with the squared amplitude of the Bessel function of order  $n$ . Image brightness adjustment is also performed by the GPU. Those maps are displayed in Fig. 3

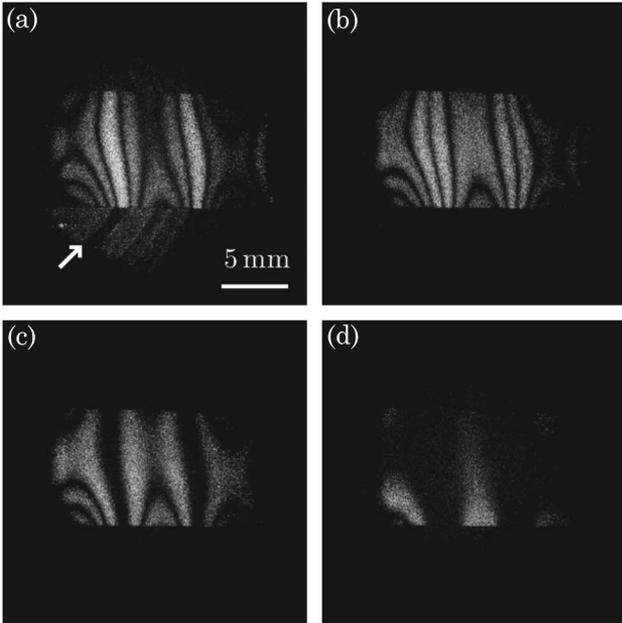


Fig. 3. Time-averaged holographic maps of the  $\omega_M/(2\pi) = 10$  kHz vibrational mode of the paper sheet for the modulation sidebands of order (a)  $n = 0$ , (b)  $n = 1$ , (c)  $n = 3$ , and (d)  $n = 7$   $1024 \times 1024$  pixels renderings. The detection sideband sweep is reported in [Media 1](#). The first modulation sideband is screened for excitation frequencies swept from 0 to 20 kHz in [Media 2](#) and from 0 to 100 kHz in [Media 3](#). The effect of the Eq. (3) filter is reported in [Media 4](#).

for the modulation sidebands of order  $n = 0$  [Fig. 3(a)],  $n = 1$  [Fig. 3(b)],  $n = 3$  [Fig. 3(c)], and  $n = 7$  [Fig. 3(d)]. Excited at  $\omega_M/(2\pi) = 10$  kHz, the paper sheet builds up a steady-state vibrational mode with rectilinear nodes and bellies oriented along  $y$ , with a mechanical wavelength of  $\sim 5$  mm. In Fig. 3(a), the nonmoving support of the object in vibration is visible (arrow). A sweep of the detection sideband is reported in [Media 1](#). Additional vibrational patterns are screened for excitation frequencies swept from 0 to 20 kHz ([Media 2](#)) and from 0 to 100 kHz ([Media 3](#)), with a detection tuned to the first modulation sideband. The propensity of the filter of Eq. (3) to cancel-out spurious artefacts is assessed in real time in [Media 4](#).

The image reconstruction and display algorithm was elaborated with Microsoft Visual C++ 2008 integrated development environment and NVIDIA's Compute Unified Device Architecture software development kit 3.2. FFT calculations were made with the function `cufftExecC2C` from the CUFFT 3.2 library on single precision floating point arrays. The program was compiled and run on Microsoft Windows 7-64 bit. The computer hardware configuration was based on an ASUS P6T motherboard with a 2.67 GHz Intel core i7 920 CPU and a NVIDIA Ge-

**Table 1. Benchmarks of Image Rendering Time**

Array Size (pixels)	Time
$1024 \times 1024$	5.5–5.9 ms
$2048 \times 2048$	19.7–20.4 ms

Force GTX 470 GPU. Image rendering calculations  $I \rightarrow H \rightarrow F \rightarrow |f|^2$  are performed sequentially, in the main GPU thread (Fig. 2); the whole processing time of one frame is reported in Table 1. For benchmark purposes, the rendering performance of  $2048 \times 2048$  pixels recordings read out at  $\omega_S/(2\pi) = 8$  Hz is also reported in Table 1.

We have demonstrated that the detection and rendering of one megapixel heterodyne holograms can be carried-out with a refreshment rate of 24 Hz with commodity computer graphics hardware. Video-rate optical monitoring of steady-state out-of-plane vibration amplitudes was reported. This demonstration opens the way to high throughput multipixel optical heterodyne sensing in real time.

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